

**Problem 3.9, page 108 in 5e Wooldridge**

The following equation describes the median housing price in a community in terms of amount of pollution (*nox* for nitrous oxide) and the average number of rooms in the houses in the community (*rooms*):

$$\log(\text{price}) = \beta_0 + \beta_1 \log(\text{nox}) + \beta_2 \text{rooms} + u$$

- (i) What are the probable signs of  $\beta_1$  and  $\beta_2$ ? What is the interpretation of  $\beta_1$ ? Explain.
- (ii) Why might *nox* [or more precise,  $\log(\text{nox})$ ] and *rooms* be negatively correlated? If this is the case, does the simple regression of  $\log(\text{price})$  on  $\log(\text{nox})$  produce an upward or downward biased estimator of  $\beta_1$ ?
- (iii) Using the data in HPRICE2.DTA, the following equations were estimated:

$$\widehat{\log(\text{price})} = 11.71 - 1.043 \log(\text{nox}), \quad n = 506, R^2 = .264$$

$$\widehat{\log(\text{price})} = 9.23 - .718 \log(\text{nox}) + .306 \text{rooms}, \quad n = 506, R^2 = .514$$

Is the relationship between the simple and multiple regression estimates of the elasticity of *price* with respect to *nox* what you would have predicted, given your answer in part (ii)? Does this mean that  $-.718$  is definitely closer to the true elasticity than  $-1.043$ ?